

**58 OTWARTE
SEMINARIUM Z AKUSTYKI**



58th Open Seminar on Acoustics

Tom II

**13-16 September 2011
Gdańsk - Jurata**

GOLAY CODED SEQUENCES IN SYNTHETIC APERTURE IMAGING SYSTEMS

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The paper presents the theoretical and experimental study of synthetic transmit aperture (STA) method combined with Golay coded transmission for medical ultrasound imaging applications. The transmission of long waveforms characterized by a particular autocorrelation function allows to increase the total energy of the transmitted signal without increasing the peak pressure. It can also improve signal-to-noise ratio and increase the visualization depth maintaining the ultrasound image resolution.

In the work the 128-element linear transducer array with 0.3 mm pitch excited by the 8 and 16-bits Golay coded sequences as well as a one cycle at nominal frequencies 4 MHz were used. The comparison of 2D ultrasound images of the tissue mimicking phantoms is presented to demonstrate the benefits of coded transmission. The image reconstruction was performed using synthetic STA algorithm with transmit and receive signals correction based on a single element directivity function.

INTRODUCTION

Ultrasound imaging has become one of the primary techniques for medical imaging mainly due to its accessibility, non-ionizing radiation, and real-time display. In ultrasonography the most commonly used image quality measures are spatial resolution and image contrast which can be determined in terms of beam characteristics of an imaging system: beam width and side-lobe level. High resolution ultrasound images can be obtained by using array transducers and advanced beam-forming techniques applying synthetic aperture (SA) imaging method. The basic idea of the SA method is to combine information from emissions close to each other. This

method is a contrast to the conventional beamforming, where only one image line is created during a transmission.

Another crucial factor for image quality in ultrasound imaging is decreasing of the signal-to-noise ratio (SNR) with depth. The severe attenuation of the ultrasonic signals in the tissue results in echoes from large depths literally buried in noise. To overcome this problem, the long wide band transmitting sequences and compression techniques on the receiver side can be applied. The average transmitted power increases proportionally to the length of the code. There are several papers in literature concerning similar boundary-condition problem of signal compression in medical diagnostic imaging [1, 2].

Till now, in SA methods it is assumed that the transmit and receive elements are the point-like sources and the dynamical focusing is realized by finding the geometric distance from the transmitting element to the imaging point and back to the receiving element. But when the element size is comparable to the wavelength the influence of the element directivity on the wave field generation and reception become significant and if ignored might be a source of errors and noise artefacts in the resulting image. In this paper the STA algorithm, which takes into account the single element directivity to improve the quality of the resulting image, is investigated. For this purpose the array element is modeled as a narrow strip transducer with a time harmonic uniform pressure distribution over its width for the far-field radiation pattern calculation. An analytical expression for the corresponding directivity function is available in literature [3]. The far-field assumption is shown to be acceptable in the considered cases of the transducer dimension to wavelength ratios. As a result the comparison of computer simulation images of the wire phantom obtained for one short cycle and Golay complementary sequences used *Field II* simulation program [4] for Matlab environment are presented. The applied coded sequences increased the visualization depth maintaining high image resolution.

1. SYNTHETIC TRANSMIT APERTURE METHOD

As an alternate to the conventional phased array imaging technique the synthetic transmit aperture (STA) method can be used [5 - 7]. It provides the full dynamic focusing, both in transmit and receive modes, yielding the highest imaging quality. In the STA method at each time one array element transmits a pulse and all elements receive the echo signals, where data are acquired simultaneously from all directions over a number of emissions, and the full image can be reconstructed from these data. The advantage of this approach is that a full dynamic focusing can be applied to the transmission and the receiving, giving the highest quality of image.

The simple model for the STA ultrasound imaging is given in Fig. 1. In transmission only a single element is used. It creates a cylindrical wave (in the elevation plane the shape of the wavefront is determined by the height of the transducer) which covers the whole region of interest. The received echo comes from all imaging directions, and the received signals can be used to create a whole image - in other words all of the scan lines can be beamformed in parallel. The created image has low resolution because there is no focusing in transmit, and therefore in the rest of this report it is called a low-resolution image. After the first low-resolution image, is acquired another element transmits and a second low-resolution image is created. After all of the transducer elements have transmitted, the low resolution images are summed and a high-resolution image is created.

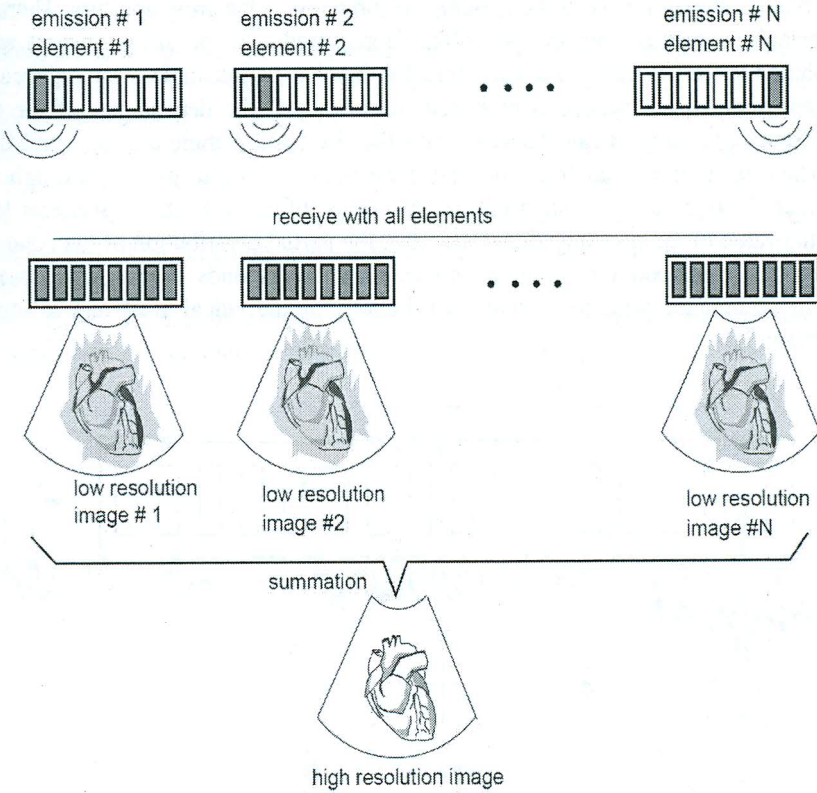


Fig.1. Low resolution images combined to produce a high resolution image [8].

In the SA ultrasound imaging methods for each point in the resulting image every combination of transmit-receive pairs contributes according to the round-trip propagation time only. The angular dependence is not taken into account in the applied point-like source model. But when the width of the array element is comparable to the wavelength corresponding to the nominal frequency of the emitted signal, the point-like source model becomes inaccurate. Here, a STA imaging algorithm, which accounts for the element directivity function and its influence [9] is applied.

The underlying idea can be illustrated on the following example, shown in Fig. 2. Here, it is assumed, that the same element transmits and receives signal. Two scatterers located at the points with polar coordinates (r_i, θ_i) , $i=1,2$ such that $r_{1m}=r_{2m}$ would contribute to the corresponding echo signal $y_{m,m}(t)$ simultaneously, since the round-trip propagation time $2r_{im}/c$, $i=1,2$ is the same. Apparently, the contribution from the scatterer at the point (r_1, θ_1) would be dominant, since the observation angle θ_{1m} coincides with the direction of maximum radiation for the m -th element, whereas its transmit-receive efficiency at the angle θ_{2m} is much smaller for the case of the scatterer at the point (r_2, θ_2) . Thereby, evaluating the value of $A(r_2, \theta_2)$, the partial contribution of the echo $y_{m,m}(t)$, in addition to the correct signal from the obstacle located at (r_2, θ_2) (being small due to the large observation angle θ_{2m}), would also introduce the erroneous signal from the scatterer located at (r_1, θ_1) . The latter signal is larger due to the small observation angle θ_{1m} . The

larger observation angles appear in the imaging region close to the array aperture. Therefore, the most appreciable deviation from the point-like source model of the array element will occur there. A solution to the problem, which accounts for the observation angle in accordance with the array element directivity function, is proposed. Assume, that the dependence of the transmit-receive efficiency of a single array element versus the observation angle is known and is denoted by $f(\theta_m)$, where θ_m is measured from the line parallel to z -axis and passing through the m -th element center. Thus, in order to suppress the erroneous influence from the scatterer located at (r_1, θ_1) on the value of the resulting signal $A(r_2, \theta_2)$, the partial contribution of the echo $y_{m,m}(t)$ is weighted by the corresponding value of $f(\theta_{2m})$. This corresponds to the superposed signal correction in accordance with respective contributions of individual scatterers located at the points (r_1, θ_1) and (r_2, θ_2) .

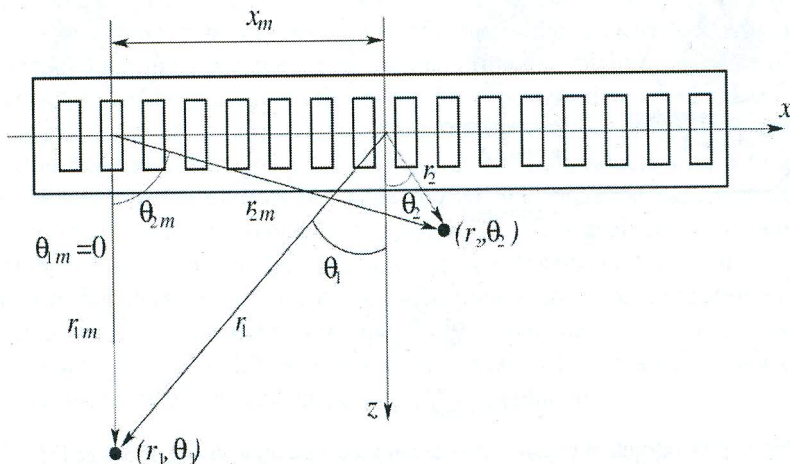


Fig.2. Influence of the scatterer located at the point (r_1, θ_1) on the value of resulting signal $A(r_2, \theta_2)$ for imaging point (r_2, θ_2) .

The above considerations lead to the following modification of the synthetic focusing imaging algorithm

$$A(r, \theta) = \sum_{m=1}^N \sum_{n=1}^N f(\theta_m) f(\theta_n) y_{m,n} \left(\frac{2r}{c} - \tau_{m,n} \right), \quad (1)$$

where $\theta_i(r, \theta)$, $i=m, n$ are the corresponding observation angles for the transmit-receive pair. The modification of the STA thus is expressed by a weighted summation of properly delayed RF signals (as in the case of conventional STA). The corresponding weights $f(\theta_m)$, $f(\theta_n)$ in the transmit and receive modes are calculated by means of the single element directivity function. Note, that the angles depend on the spatial location of the imaging point (r, θ) . The directivity function $f(\theta)$ can be calculated in the far-field approximation for a single element of the array transducer in analogous manner as in [3]

$$f(\theta) = \frac{\sin(\pi d / \lambda \sin \theta)}{\pi d / \lambda \sin \theta} \cos \theta, \quad (2)$$

where d is the element width, and λ is the wavelength.

2. GOLAY COMPLEMENTARY SEQUENCES

Among the different excitation sequences proposed in ultrasonography, Golay codes evoke more and more interest in comparison with other signals. The reason of that lies in the fact that Golay codes, like no other signals, suppress to zero the amplitude of side-lobes. This type of complementary sequences has been introduced by Golay [10]. The pairs of Golay codes belong to a bigger family of signals, which consist of two binary sequences of the same length n , whose auto-correlation functions have the side-lobes equal in magnitude but opposite in sign. The sum of these auto-correlation functions gives a single auto-correlation function with the peak of $2n$ and zero elsewhere [11].

Fig. 3 shows the pair of complementary Golay sequences, their autocorrelations, and the zero side-lobes sum of their autocorrelations.

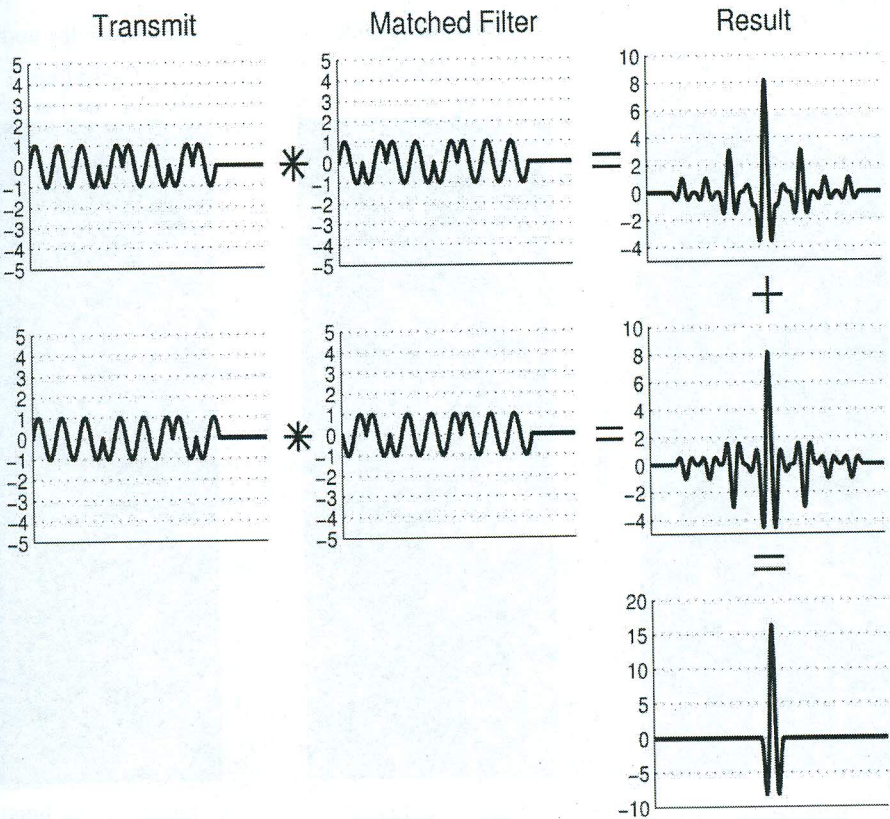


Fig.3. Principle of side-lobes cancellation using pair of Golay complementary sequences of length 8 bits.

As can be seen from the Fig. 3, the key to side-lobes canceling property of Golay code pairs is that the range side-lobes of one are equal in amplitude and opposite in sign to the side-lobes of the other.

3. COMPUTER SIMULATION

Simulations in this work are carried out with a powerful software, *Field II* that runs under Matlab.

In Fig. 4 a computer simulation of multi-scatterers phantom when a 128-element linear transducer array with 0.3 mm pitch was applied is shown. The one cycle as well as the pairs of complementary Golay sequences of the lengths 8 and 16 bits at nominal frequency 4 MHz were used. The phantom attenuation is equal to 0.5 dB/[MHz×cm]. The element pitch is about λ , where λ corresponds to the nominal frequency of the burst pulse. In the applied STA algorithm the element directivity correction scheme, discussed in [9], was implemented to improve the image quality near transducer aperture. The transmit and receive elements combinations give a total of 128×128 possible RF A-lines. All these A-lines echo signals are sampled independently at a frequency of 40 MHz and stored in RAM.

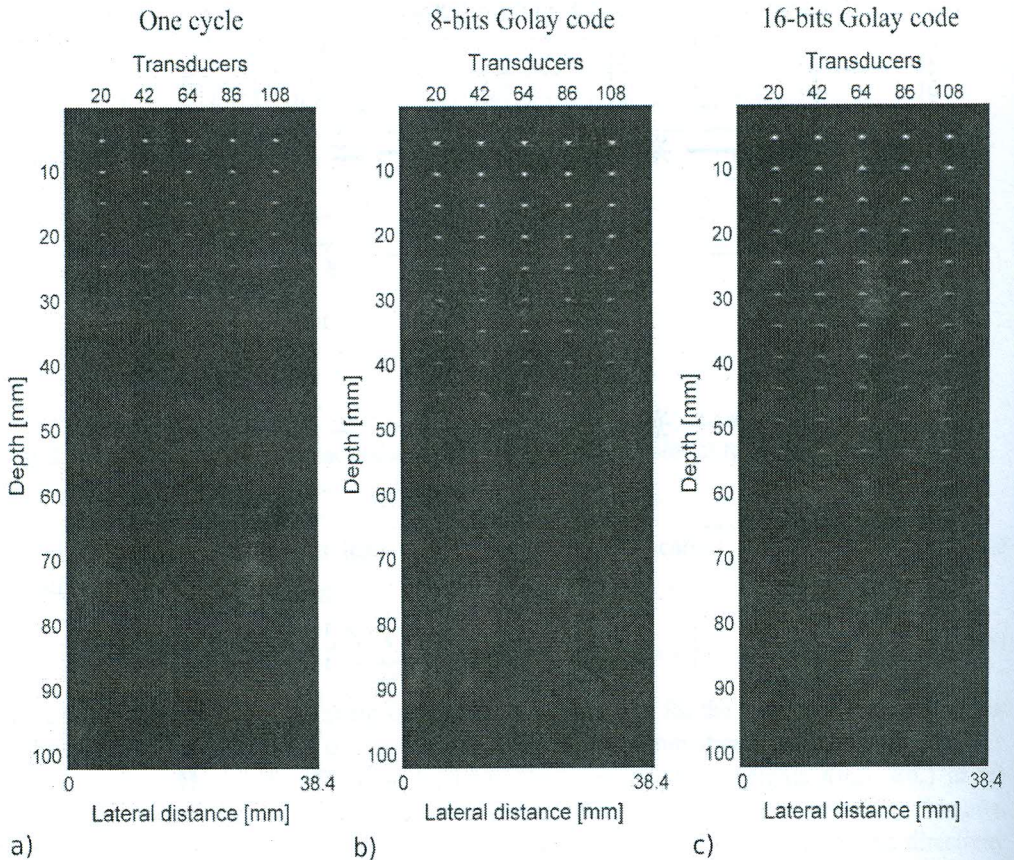


Fig.4. Comparison of 2D ultrasound images obtained by computer simulation for 128-element linear array using: a) one cycle; b) 8-bits Golay sequences; c) 16-bits Golay sequences. The phantom attenuation is equal to 0.5 dB/[MHz×cm].

The obtained 2D ultrasound images clearly demonstrate the advantage of using the Golay coded sequences. With the elongation of the coded sequences the acoustical power increases yielding a higher SNR, that leads to an increase in the penetration depth while maintaining both axial and lateral resolution. The latter depends on transducer acoustic field and is discussed in [12]. The visualization depth when the one cycle was applied is equal to 3 cm (Fig. 4a), while in case of applying 8-bits Golay codes this depth increases to 5 cm (Fig. 4b), and for longer 16-bits Golay codes this depth of visualization increases up to 7 cm (Fig. 4c).

In order to compare the lateral resolution the cross section of phantom at a depths of 10 mm and 30 mm is shown in Fig. 5. Note, the normalization is performed with respect to the maximum values of the corresponding cross sections at different depth.

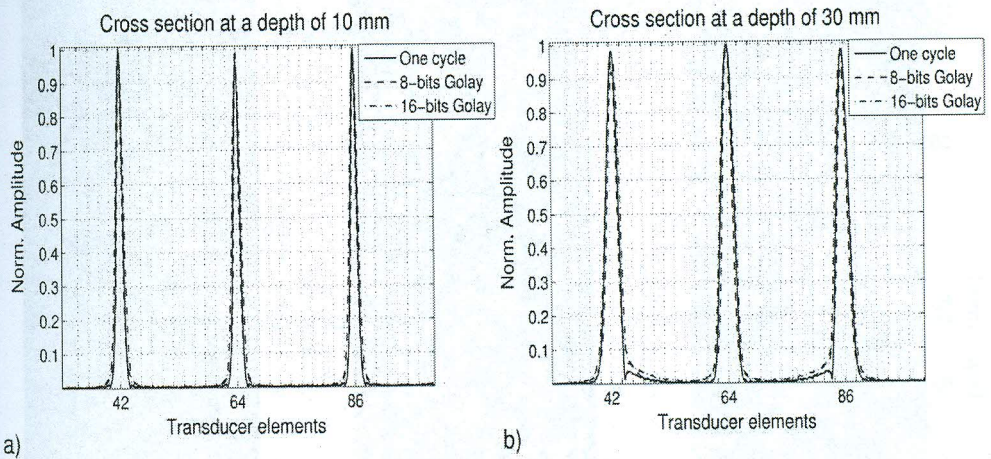


Fig.5. Comparison of the lateral resolution at a depths of 10 mm (a) and 30 mm (b) when one cycle, 8 and 16-bits Golay sequences were applied.

In Fig. 5 it can be seen that the lateral resolution at the different depths for all burst signals is the same.

4. EXPERIMENTAL RESULTS AND DISCUSSION

The 128-element linear transducer array with 0.3 mm pitch excited by the 8 and 16-bits Golay coded sequences as well as a one cycle at nominal frequencies 4 MHz were used in the experiments. A single element in the transducer transmitting aperture was used to generate an ultrasound wave covering the full image region. All elements were used for both transmitting and receiving. The RF echo signals sampled independently at 40 MHz and processed by the STA algorithm. Experimental data were acquired by an Ultrasonix - SonixTOUCH Research System (Ultrasonix Medical Corporation, Canada).

The tissue mimicking phantom model 525 Danish Phantom Design with attenuation of background material 0.5 dB/[MHz×cm] was used. It consists of several nylon filaments twists 0.1 mm in diameter positioned every 1 cm axially. This phantom allows to examine the axial and lateral resolution at various depths in the ultrasound image.

The comparison of the 2D ultrasound images of the tissue phantom obtained for one cycle, 8-bits and 16-bits Golay complementary sequences is shown in Fig. 6. The peak pressure level of excitation signals at the transducer were set as low as possible to visually detect the echoes received using one cycle burst transmission slightly larger than the noise level. The same peak pressure has been used for the coded transmission.

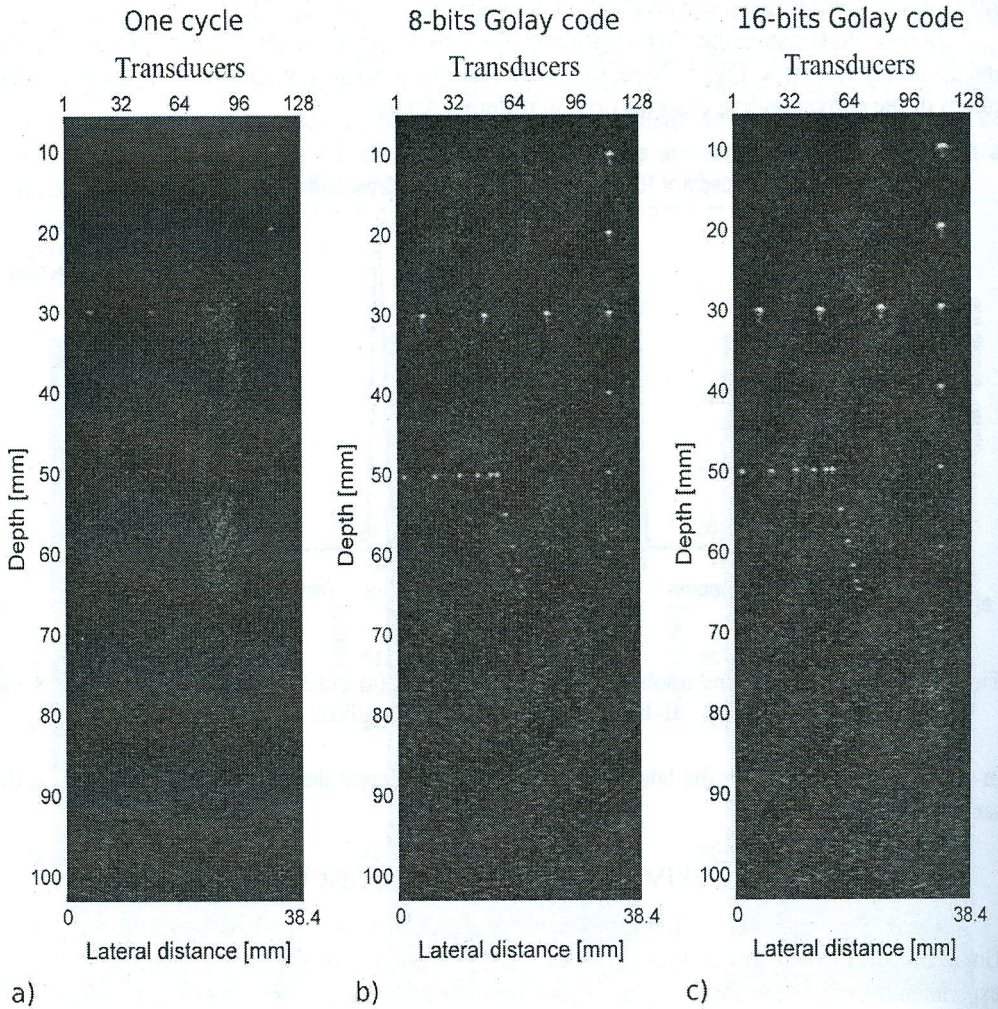


Fig.6. 2D ultrasound images of tissue mimicking phantom using: (a) one cycle; (b) 8-bits Golay code; (c) 16-bits Golay code.

The obtained 2D ultrasound images show an excellent performance of the coded excitation in terms of increasing penetration depth. In the case of one cycle the penetration depth is equal only to 3cm (Fig. 6a). In the case of 8-bits Golay code the penetration depth increases up to 7 cm (Fig. 6b). With the elongation of the coded sequences to 16 bits the acoustical power increases

yielding higher SNR, that leads to an increase in the penetration depth up to 8 cm (Fig. 6c). Note that axial and lateral resolution is the same for the all burst signals.

In order to compare quantitatively the SNR gain the 112th line from 128 RF-lines of the 2D ultrasound images is shown in Fig. 7 and the SNR is calculated. For this purpose the noise level which appeared straight after the signal was chosen.

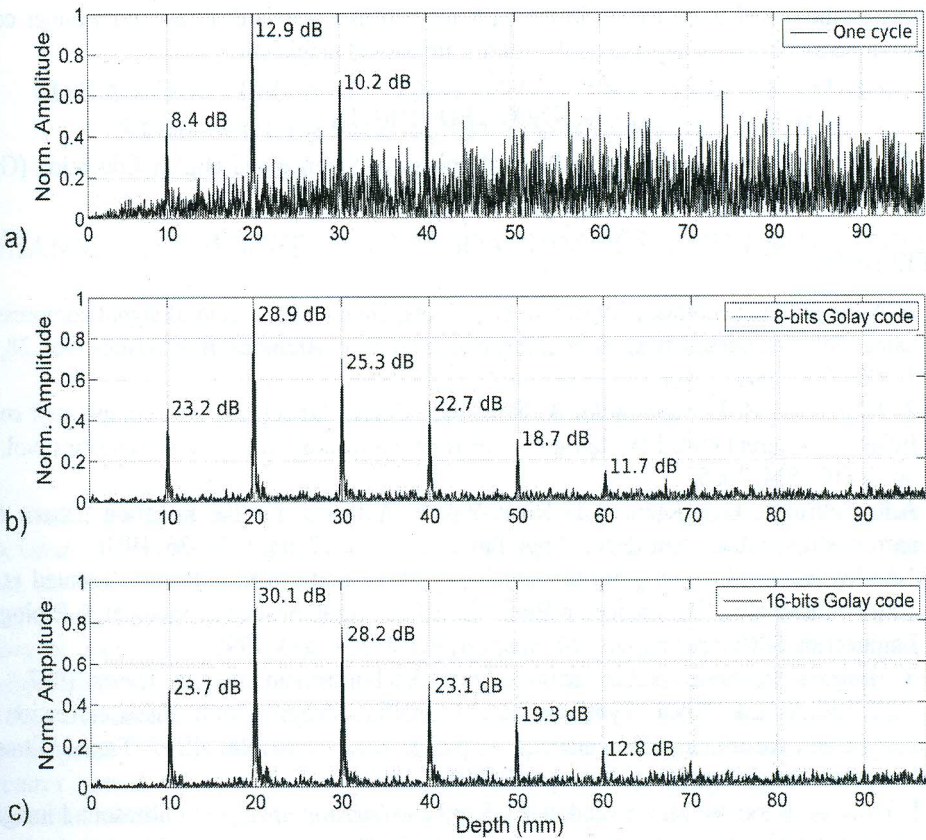


Fig.7. The RF-lines of the tissue mimicking phantom using: a) one cycle; b) 8-bits Golay code; c) 16-bits Golay code.

Fig. 7 shows that applying coded transmission in comparison to one cycle pulse allows to improve the SNR by about 15 dB. Elongating coded transmission two times the SNR increases by about 1.4 dB which is in agreement with studies shown in [11]. The SNR increase in its turn leads to improvement of the penetration depth and the contrast of the image.

5. CONCLUSION

Ultrasound imaging allows to visualize structures and organs in real-time, enabling an instantaneously evaluation of clinical situation. But real problems appear when the reconstruction of the deeply located organs is needed. For that reason, coded excitation was used making

examination procedure more precise and allowing visualization of the deeply located organs in 2D B-mode ultrasound imaging.

This work has addressed the problems in medical ultrasound imaging: improving of the penetration depth and gaining the SNR. To solve these problems, the complementary pairs of Golay coded sequences were used. The comparison of the 2D ultrasound images show that elongated coded sequences from 8-bits to 16-bits increase the penetration depth by about 2 cm. Applying of the coded transmission in the STA method in a standard ultrasound scanner could allow to increase the efficiency and quality of the ultrasound diagnostic.

ACKNOWLEDGMENTS

This work was supported by the Polish Ministry of Science and Higher Education (Grant NN518382137).

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