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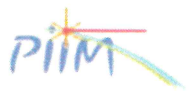
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Periodic Behavior of an Anisotropic Trumbbell Settling Under Gravity

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We will present a study of a V-shaped rigid conglomerate of three spherical particles of the same radii (trumbbell), which settles under gravity in a viscous fluid. The side spheres have equal masses, but the middle sphere has a different mass and touches the other ones. The configuration of the trumbbell is parametrized by the apex angle α (generally, the side spheres do not touch each other). Previous studies (1) shows that a trumbbell with equal masses orients itself towards a stable stationary configuration. However, recent results regarding natural sediment flocs(2) as well as the settling process of a rigid U-shaped disk (3) under gravity show that an anisotropic mass distribution might lead to quasi-periodic evolution of the system.

In our case, translational \mathbf{U} and rotational Ω velocities of the rigid conglomerate are linear functions of the total force \mathbf{F} acting on the conglomerate:

$$\mathbf{U} = \underline{\underline{\mu}}^{\{tt\}} \cdot \mathbf{F}, \quad \Omega = \underline{\underline{\mu}}^{\{rt\}} \cdot \mathbf{F}$$

where \mathbf{U} is the velocity of the conglomerate center-of-mass, and the mobility tensors $\underline{\underline{\mu}}^{\{tt\}}$ and $\underline{\underline{\mu}}^{\{rt\}}$ are calculated in the CMS frame of reference in which torque vanishes. For

$\theta = \phi = \psi = 0$, $\underline{\underline{\mu}}^{\{tt\}}$ is the diagonal 3×3 matrix and only non-zero components of $\underline{\underline{\mu}}^{\{rt\}}$ are $\underline{\underline{\mu}}^{\{rt\}}_{\{yx\}} = -\mu_a$ as well as $\underline{\underline{\mu}}^{\{rt\}}_{\{xy\}} = \mu_b$. The hydrodynamic interactions are essential in this problem, and we find the components of the mobility tensor using precise HYDROMULTIPOLE codes for the multipole expansion (4) with the truncation at $L=8$.

We find that trumbbells with the anisotropic mass distribution show qualitatively different long-time dynamics than those with equal masses. When $\mu_a \cdot \mu_b < 0$, the system shows instability towards the long-time periodic motion.

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(2) K. Spencer et al., *Water Research* **222**, 118835 (2022)

(3) T. Miara et al., *Commun. Phys.* **7**, 47 (2024)

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